

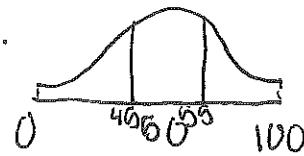
AMS +  
Lecture 4  
6/27/16

New Draper Office Hours: MWF 11:45-12:45  
BE 367C

Standard Deviation:

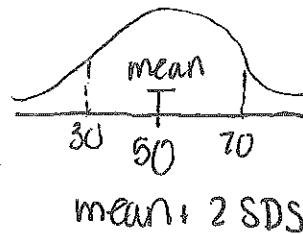
Empirical Rule: helps to estimate SD

ex.

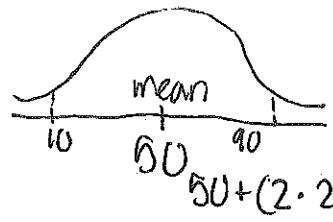


SD 5? too small

SD 60? too large (all graph)



Should be ~95%: no, still  
too small



SD = 20, looks about right

Empirical Rule for estimating SD

always starting at the mean:

go 1 SD either way

go 2 SD either way

go 3 SD either way

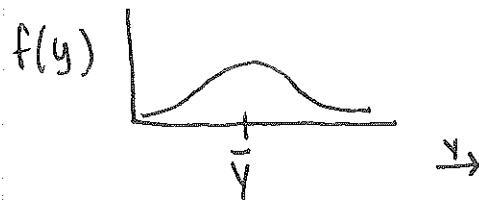
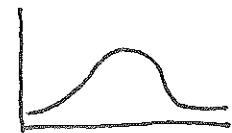
should capture:

2/3 of data, 68%

most/95% of data

all 99.7% of data

## Normal Curve / Gaussian Distribution

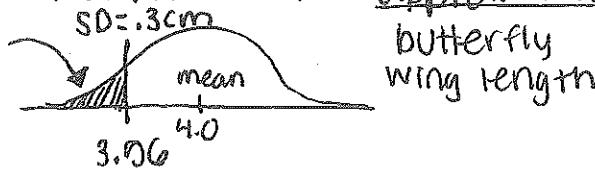


ex. LOOKING at our butterfly data set -  
What %  $\leq 3.56$  cm? ~8%

$$\text{count } 2/24 = 8.3\%$$

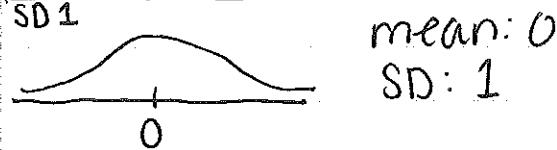
this is the exact answer

if we want the approximate answer:

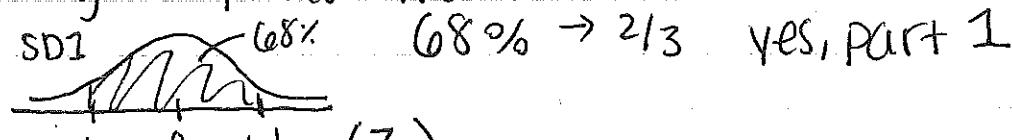


The normal curve is dependent on the value of the mean and the SD.

## Standard Normal Curve

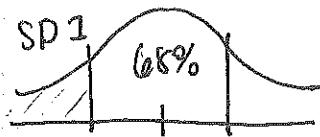


USING Empirical Rule



{See pages L-34 and L-36 for Standard Normal Table. Table gives decimals}

- FACTS:
1. all normal curves are symmetric
  2. total area under each normal curve is 100% = 1
  3. ALL normal curves satisfy emp. rule exactly



Negative  $\rightarrow$   $-1 \quad 0 \quad 1$

value:  $-1.00$

from table: .1587

table gives decimal  
 $= 15.87\% \approx 16\%$

BC curve is symmetric,  
area to left  $-1 =$  area  
right of  $+1$ ; both  $= 16\%$

Total area must add up  
to 100%.

value for the area  
 $100\% - (2 \cdot 16\%) = 68\%$

To calculate the actual  
value for the area under curve  $[t_1, t_2]$

Positive



value:

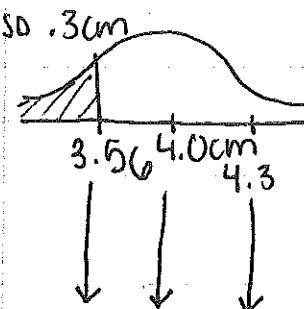
from table:  $.8413 = 84\%$

$\leftarrow 16\% \quad \rightarrow 16\%$

$84\% - 16\% = 68\%$

should  
be equal!

ex



Wing Length

Y (in raw units)

$X \rightarrow 0 \quad +1 \quad (\text{standard units } z)$

RAW

$\downarrow$   
Standard

$$X = \frac{3.56 \text{ cm} - 4.00 \text{ cm}}{0.3 \text{ cm}} = \frac{\# - \text{mean}}{\text{SD}} = \frac{-0.44}{0.3} = -1.47 = X$$

converting to std units

$$\frac{Y - \bar{Y}}{S}$$

note: units should cancel, no  
units

So now we want to know area to left  
of  $-1.47$ .

Using negative chart,  
 $-1.4 \quad .07 \rightarrow .0708 \approx 7\%$



## Section 2: Experimental Design

L-67

Controlled Experiment = control group (C) and a treatment group (T), and the experimenters control who goes into which groups).

"Is this difference practically significant?"

Comparing Data ① absolute

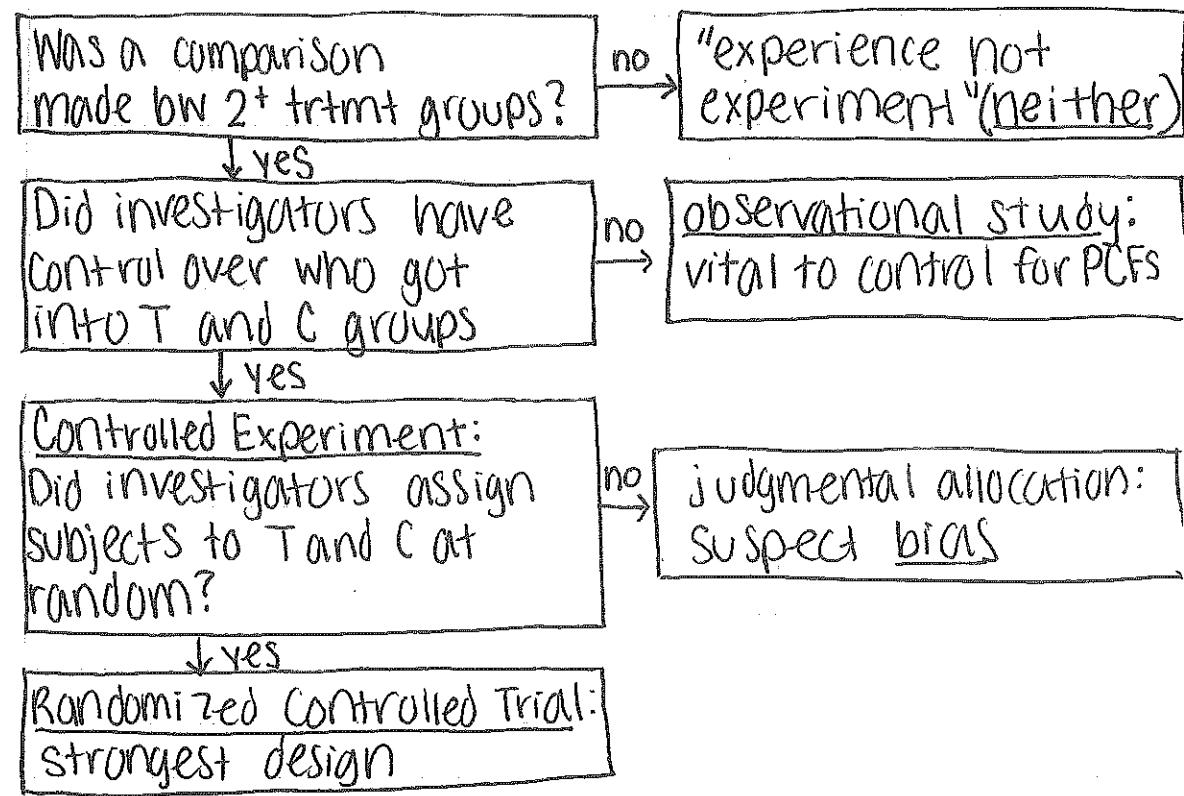
② percentage

We want the subjects in T to be similar to C (as similar as possible) in all relevant ways except for the T/C distinction

To encourage similarity: randomize

→ Randomized Controlled Trial (RCT) Experiment

## Flowchart for Classifying Experimental Designs



Bias: systematic tendency to over/underestimate the truth

## BACK TO THE CORTEX EXPERIMENT

- Y outcome : cortex weight
- X treatment : T vs C 1/0
- Z potential confounding factor (PCF) : genetic background (cortex weight)

Positively Associated:  $u \uparrow, v \uparrow$  on avg (+viceversa)

Negatively Associated:  $u \uparrow, v \downarrow$  "

PCF: in an experimental setting w/ treatment variable X and outcome variable Y, any third variable Z may plausibly be associated both w/ X and Y

ex. Y (outcome) : cortex weight    X (trtmnt) <sup>T: enriched</sup> <sub>C: depriv</sub>

Z (genetics)

as  $Z \uparrow Y \uparrow$  ✓

as  $X \rightarrow T, Z \uparrow \downarrow$  ✓

PCFs are the enemy in experimental design bc they cause bias in conclusions.

How to defeat PCFs?

HOLD them CONSTANT in T/C comparison.